



DEVELOPMENT OF A CUSTOM INDUCTION MACHINE COMPONENT FOR COMPUTATIONALLY EFFICIENT FLYWHEEL ENERGY STORAGE SIMULATION

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TABLE OF CONTENTS

- Introduction
- Custom IM model description
- Model efficiency
- Simulation results
- Conclusions

INTRODUCTION

Background information

- Effect of distributed energy storage devices with dissimilar response times is investigated
- A medium voltage test network, with embedded energy storage systems (ESS), central controller and telecommunications emulation is considered
- A modified version of the CIGRE European MV distribution network, with number of ESS is to be implemented
- A combination of at least 12 ESS will be included
- A delay model for telecommunications emulation will be included
- Real-time simulation should be realised
- A set of two racks with 5 PB5 are available for testing

INTRODUCTION

Motivation

- A low-speed flywheel energy storage system (FESS) is to be used
- An ideal, symmetric induction machine is sufficient for the FESS
- Saturation effects and zero-sequence components can be neglected
- A detailed representation of the FESS transient response is required for benchmarking
- Multiple FESS (up to twelve) are to be considered
- Local connection to the MV network buses is assumed
- Time-step of the system need to be compatible with the rest of the system

INTRODUCTION

Induction Machine models in RTDS

- DQ0 model
 - Highly efficient
 - Known to have poor accuracy at large time-steps
- Phase-Domain (PD) model
 - More accurate than the DQ model at large time-steps
 - Its time-varying inductance matrix make it considerably more computing intensive
- Phase-Domain Light (PD-L) model
 - Analytically inverted matrix improves computer efficiency over the PD model
 - Less efficient than the DQ model

INTRODUCTION

Hybrid IM models

- Combine PD and DQ0 quantities on their formulation to improve on the PD model efficiency
- Depending on choice of state-space variables of the differential equation from where the model is derived, different numerical properties are obtained: they may be more accurate than the PD model at large time-steps.
- Machine speed may still be present in some hybrid model's conductance matrix. Approximation can be used to eliminate speed dependency with negligible error.
- Hybrid models derived from the classical PD model (using stator and rotor flux linkages as state variables) have a constant conductance matrix, with no approximations, if saturation is neglected.

MACHINE MODEL DESCRIPTION

Hybrid custom model – base differential equations

- Saturation effects are neglected

$$V = p\psi + RI$$

State-space form

$$p\psi = -RL^{-1}(\theta)\psi - V$$

Where:

$$V = [V_{abcs} V_{abcr}]^T$$

$$\psi = [\psi_{abcs} \psi_{abcr}]^T$$

$$I = [I_{abcs} I_{abcr}]^T$$

$$R = \text{diag}[R_s R_r]$$

MACHINE MODEL DESCRIPTION

PD Inductance matrices

And:

$$\mathbf{L}(\theta) = \begin{bmatrix} \mathbf{L}_{ss} & \mathbf{L}_{sr}(\theta) \\ \mathbf{L}_{sr}^T(\theta) & \mathbf{L}_{rr} \end{bmatrix}$$

$$\mathbf{L}_{ss} = \begin{bmatrix} L_{ls} + L_{ms} & -\frac{1}{2}L_{ms} & -\frac{1}{2}L_{ms} \\ -\frac{1}{2}L_{ms} & L_{ls} + L_{ms} & -\frac{1}{2}L_{ms} \\ -\frac{1}{2}L_{ms} & -\frac{1}{2}L_{ms} & L_{ls} + L_{ms} \end{bmatrix}$$

$$\mathbf{L}_{rr} = \begin{bmatrix} L_{lr} + L_{mr} & -\frac{1}{2}L_{mr} & -\frac{1}{2}L_{mr} \\ -\frac{1}{2}L_{mr} & L_{lr} + L_{mr} & -\frac{1}{2}L_{mr} \\ -\frac{1}{2}L_{mr} & -\frac{1}{2}L_{mr} & L_{lr} + L_{ms} \end{bmatrix}$$

$$\mathbf{L}_{sr}(\theta) = \begin{bmatrix} L_{sr} \cos \theta_r & L_{sr} \cos \left(\theta_r + \frac{2\pi}{3} \right) & L_{sr} \cos \left(\theta_r - \frac{2\pi}{3} \right) \\ L_{sr} \cos \left(\theta_r - \frac{2\pi}{3} \right) & L_{sr} \cos \theta_r & L_{sr} \cos \left(\theta_r + \frac{2\pi}{3} \right) \\ L_{sr} \cos \left(\theta_r + \frac{2\pi}{3} \right) & L_{sr} \cos \left(\theta_r - \frac{2\pi}{3} \right) & L_{sr} \cos \theta_r \end{bmatrix}$$

MACHINE MODEL DESCRIPTION

Custom model - EMTP-Type form

Voltage equations

$$\mathbf{V}_{abc}(t) = \mathbf{R}_{equ}^{FF} \mathbf{I}_{abc}(t) - \frac{3}{2} \frac{Z_M}{\Delta t} \mathbf{I}_0 + \mathbf{E}_{equ}^{FF}(t)$$

$$\mathbf{R}_{equ}^{FF} = \frac{2}{\Delta t} \mathbf{L}_{eq}^{FF} + \mathbf{R}_s \quad \mathbf{I}_0 = [i_0 \quad i_0 \quad i_0]^T$$

$$\mathbf{L}_{eq}^{FF} = \begin{bmatrix} L_{ls} + Z_M & 0 & 0 \\ 0 & L_{ls} + Z_M & 0 \\ 0 & 0 & L_{ls} + Z_M \end{bmatrix}$$

$$\mathbf{E}_{equ}^{FF}(t) = \frac{2}{\Delta t} \mathbf{T}^{-1}(t) \mathbf{L}_{srdq} \mathbf{E}_{rhis} - \mathbf{E}_{shis}$$

Auxiliary expressions

$$i_0 = \frac{i_a + i_b + i_c}{3}$$

$$\mathbf{E}_{shis} = \mathbf{V}_{abc}(t - \Delta t) - \mathbf{R}_s \mathbf{I}_{abc}(t - \Delta t) + \frac{2}{\Delta t} \mathbf{\Psi}_{abc}(t - \Delta t)$$

$$\mathbf{E}_{rhis} = \mathbf{E}_{rr}^{-1} \mathbf{L}_{rsdq} \mathbf{I}_{dq0s}(t - \Delta t) + \frac{\Delta t}{2} \mathbf{E}_{rr}^{-1} \left(\mathbf{V}_{dq0r}(t) + \mathbf{V}_{dq0r}(t - \Delta t) + \frac{2}{\Delta t} \mathbf{E}_{rr}^* \mathbf{I}_{dq0r}(t - \Delta t) \right)$$

$$\mathbf{E}_{rr} = \mathbf{L}_{rrdq} + \frac{\Delta t}{2} \mathbf{R}_r \quad \mathbf{E}_{rr}^* = \mathbf{L}_{rrdq} - \frac{\Delta t}{2} \mathbf{R}_r$$

$$Z_M = L_M(1 - Z_{mm}) \quad Z_{mm} = \frac{L_M}{L_M + L_{rns}} \quad L_{rns} = L_{lr} + \frac{1}{\Delta t} r_r$$

$$\mathbf{L}_{ssdq} = \begin{bmatrix} L_{ls} + L_M & 0 & 0 \\ 0 & L_{ls} + L_M & 0 \\ 0 & 0 & L_{ls} \end{bmatrix} \quad \mathbf{L}_{srdq} = \begin{bmatrix} L_M & 0 & 0 \\ 0 & L_M & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\mathbf{L}_{rrdq} = \begin{bmatrix} L_{lr} + L_M & 0 & 0 \\ 0 & L_{lr} + L_M & 0 \\ 0 & 0 & L_{lr} \end{bmatrix} \quad \mathbf{L}_{rsdq} = \mathbf{L}_{srdq}^T$$

DQ matrices

$$T_e = \frac{3P}{2} (\psi_{as} i_{qs} - \psi_{qs} i_{as})$$

Mechanical equations

$$\omega_r(t) = \omega_r(t - \Delta t) + \frac{\Delta t P}{2} [T_e(t) + T_e(t - \Delta t) - 2T_m]$$

$$\theta_r(t) = \theta_r(t - \Delta t) + \frac{\Delta t}{2} [\omega_r(t) - \omega_r(t - \Delta t)]$$

D. S. Vilchis-Rodriguez and E. Acha, "Nodal Reduced Induction Machine Modeling for EMTP-Type Simulations," in *IEEE Transactions on Power Systems*, vol. 27, no. 3, pp. 1158-1169, Aug. 2012, doi: 10.1109/TPWRS.2012.2186987.

MACHINE MODEL DESCRIPTION

Custom model - RSCAD implementation

Neglecting zero-sequence component, the model is interfaced by using:

$$\mathbf{I}_{abcS}(t - \Delta t) = \mathbf{G}\mathbf{V}_{abcS}(t - \Delta t) + \mathbf{IH}_S$$

Where:

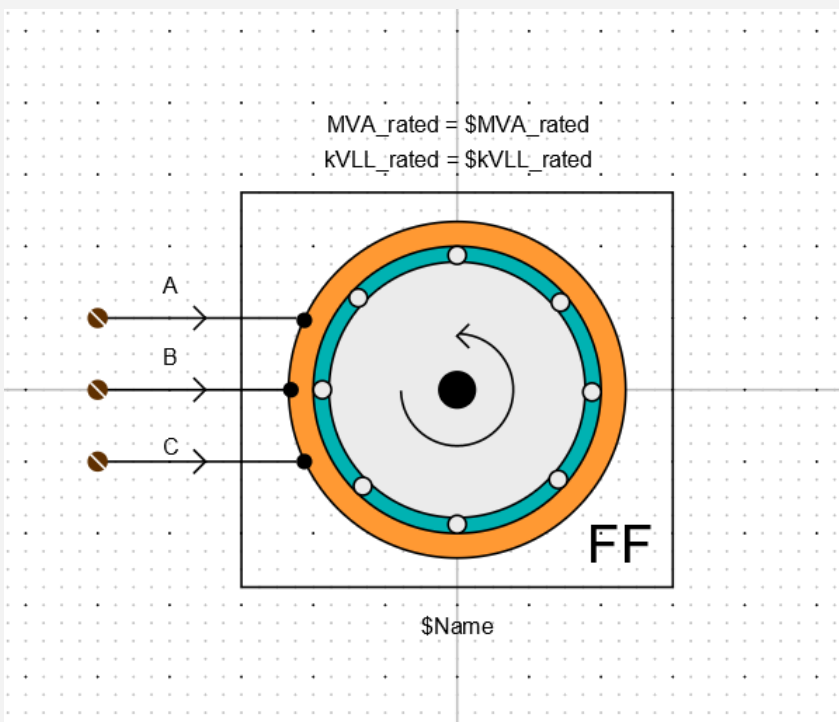
$$\mathbf{G} = \mathbf{R}_{equ}^{FF}{}^{-1}$$

and the injected currents are defined by

$$\mathbf{IH}_S = -\mathbf{G}\mathbf{E}_{equ}^{FF}(t - \Delta t)$$

MACHINE MODEL DESCRIPTION

Custom model - RSCAD implementation



- Angle prediction-correction scheme is employed in the model solution

$$\theta_r(t) = 2\theta_r(t - \Delta t) - \theta_r(t - 2\Delta t)$$

$$\theta_r(t) = \theta_r(t - \Delta t) + \frac{\Delta t}{2} [\omega_r(t) - \omega_r(t - \Delta t)]$$

- 94 flops (+, -, x) required for the model solution. Divide operations are completely avoided
- 2 trigonometric functions are also required

MACHINE MODEL DESCRIPTION

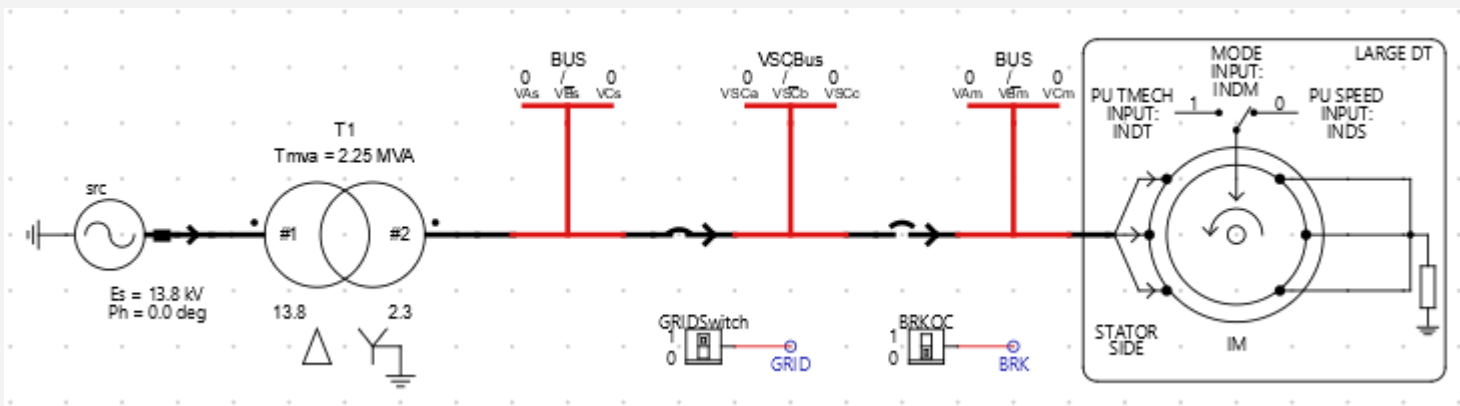
Custom model - RSCAD implementation

| | Name | Description | Value | Unit | Min | Max |
|----------------------|------------|---------------------------|--------------------------------------|--------|-----|-----|
| CONFIGURATION | fbase | Rated frequency | <input type="text" value="\$fbase"/> | Hz | | |
| Motor parameters | MVA_rated | Rated power | <input type="text" value="\$Pbase"/> | MVA | | |
| Monitoring | kVLL_rated | Rated L-L voltage | <input type="text" value="\$VII"/> | kV | | |
| Signals Names | Poles | Poles number | <input type="text" value="\$Poles"/> | number | | |
| PROCESSOR ASSIGNMENT | LlsPU | Stator leakage inductance | <input type="text" value="\$LlsPU"/> | pu | | |
| | LlrPU | Rotor leakage inductance | <input type="text" value="\$LlrPU"/> | pu | | |
| AUTO-NAMING SETTINGS | LmPU | Magnrtizing inductance | <input type="text" value="\$LmPU"/> | pu | | |
| | RsPU | Stator resistance | <input type="text" value="\$RsPU"/> | pu | | |
| | RrPU | Rotor resistance | <input type="text" value="\$RrPU"/> | pu | | |
| | J | Inertia | <input type="text" value="\$J"/> | kg.m^2 | | |

- Machine parameters are provided in p.u.
- Stator currents, electromagnetic torque, machine speed and rotor angle can be monitored.
- To avoid additional calculations, input/output voltages and currents are handled natively in kV and kA.
- Calculation of rotor currents is omitted to reduce flop count.

MODEL EFFICIENCY

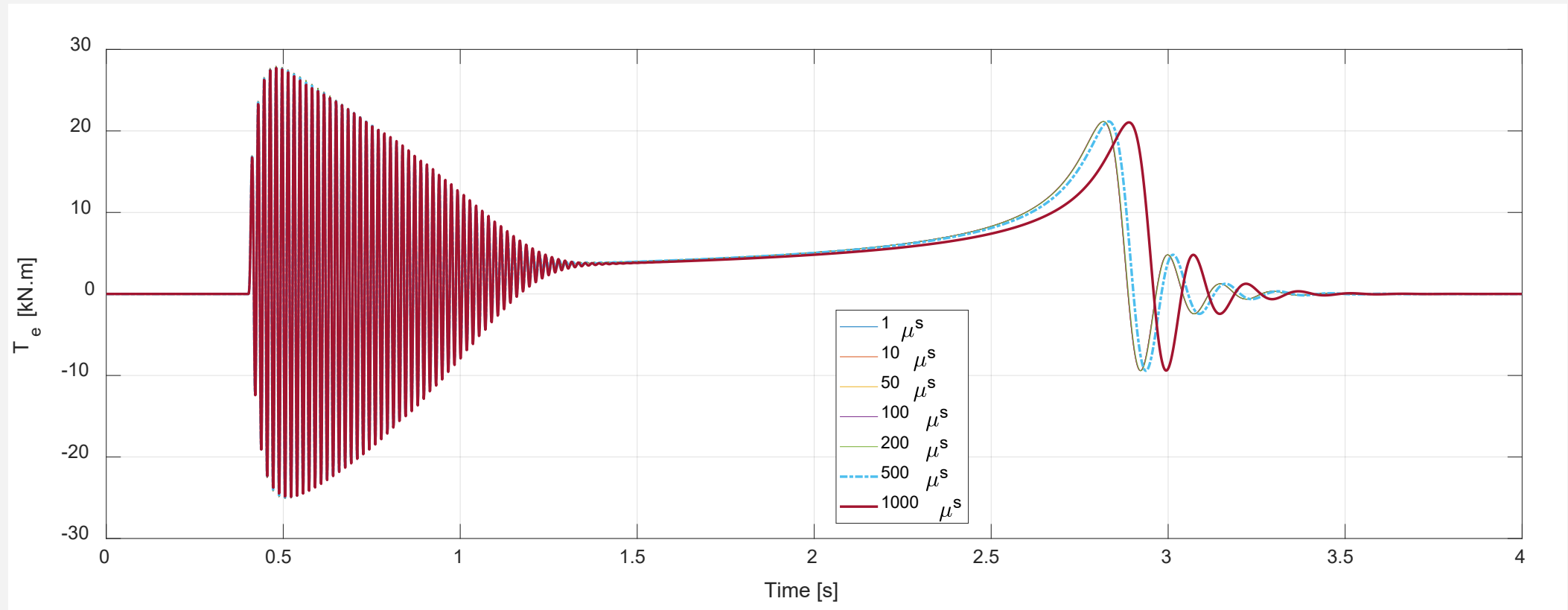
Test system



- Simple system used to verify the custom model results and performance. Startup transient is used for the assessment.
- An RTDS stack with five PB5 was used in the tests.
- For the case under test, identical load was reported for the custom model and RSCAD's DQ0 model (15% of a PB5), 22% for PD and 18% for PD-light.
- Minimum time-step at which real-time simulation was achievable for the custom and RSCAD's DQ0 model was identical (8 μ s), PD-light 14 μ s and 15 μ s for the PD.

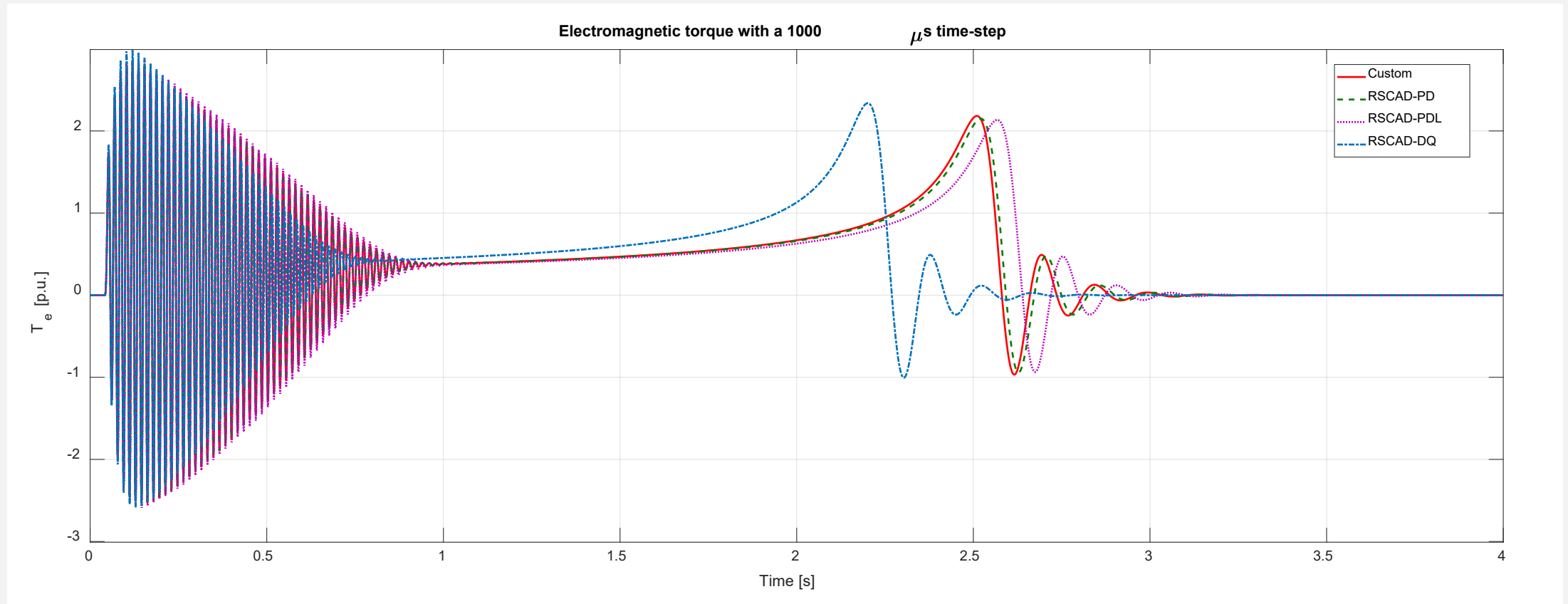
SIMULATION RESULTS

Time-step length effect



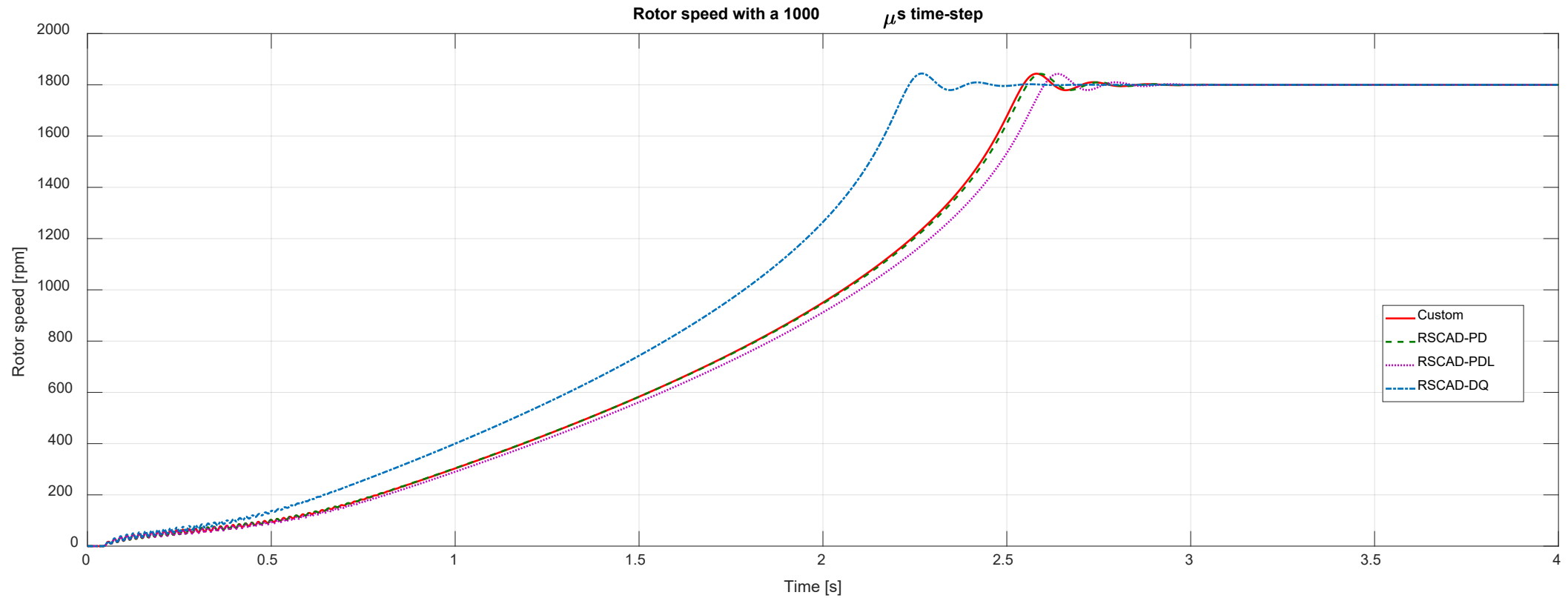
SIMULATION RESULTS

Time-step length effect



SIMULATION RESULTS

Time-step length effect



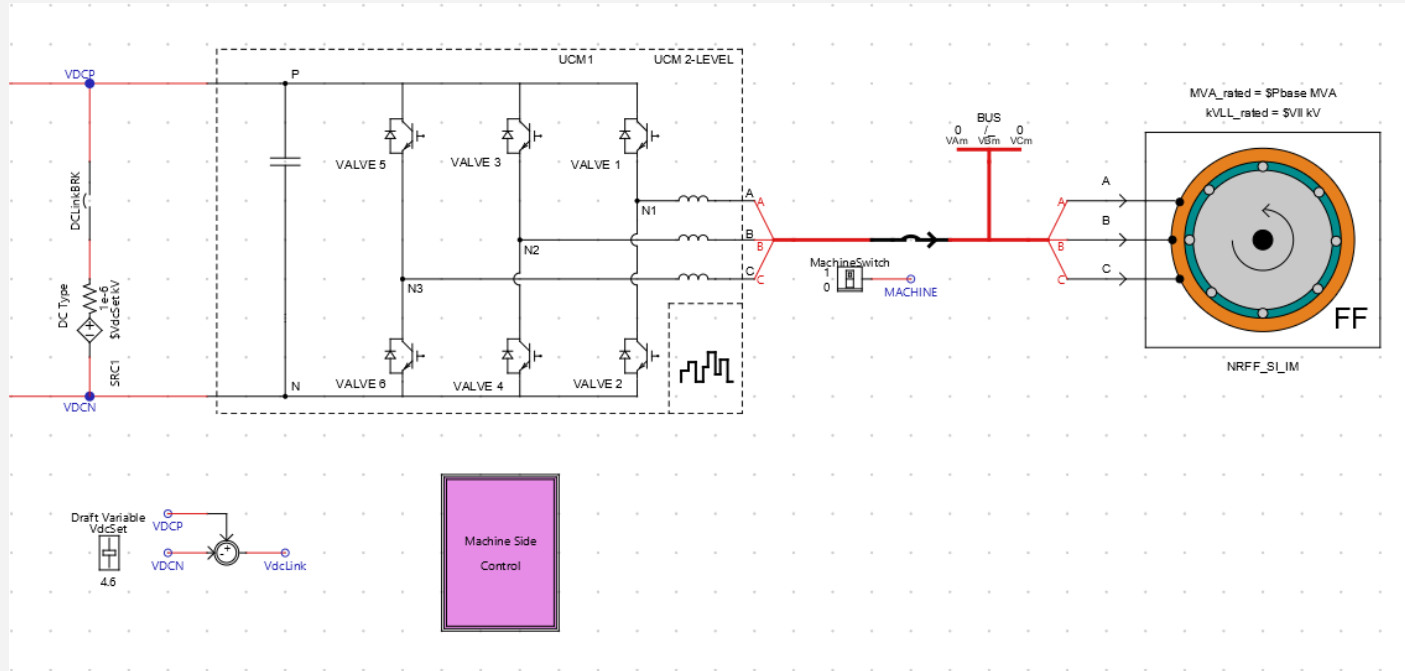
MODEL EFFICIENCY

Summary - models performance

| Model | Load [%] | Time-step [μ s] | Notes |
|--------|-----------|----------------------|---|
| PD | 22 (+47%) | 15 (+88%) | The most computing intensive |
| PD-L | 18 (+20%) | 14 (+75%) | Slightly more efficient than the PD model, diverges from the PD model at large time-steps |
| DQ0 | 15 (base) | 8 (base) | Very efficient but poor accuracy at large time-steps |
| Custom | 15 (+0%) | 8 (+0%) | As efficient as the DQ0 and as accurate as the PD model |

SIMULATION RESULTS

Custom model - FESS integration



- The custom model has been incorporated into a FESS
- Computing load is identical to that of the FESS using RSCAD's DQ model (27% of a PB5), the PD model uses 35%.
- Minimum time-step at which real-time simulation is realizable is identical to that of the DQ0 model ($16\mu\text{s}$). The PD model requires $23\mu\text{s}$ (+44%).
- Computing time (off-line), to complete an 18.5 s simulation at $1\mu\text{s}$ time-step with the UCM in improved firing pulse mode is similar to the obtained using the DQ model.

CONCLUSIONS

- A custom induction machine component for RSCAD/RTDS, with direct interface with the power network, was implemented.
- By neglecting magnetic saturation and zero sequence components a constant, diagonal conductance matrix is obtained.
- The model was found to have similar computing performance to that of RSCAD's DQ model.
- Error propagation with increase in time-step length was found to be very similar to RSCAD's PD model
- RSCAD's PD-L results were found to diverge from that of the conventional PD model for large time-steps.
- The combined use of PD and DQ quantities, and avoiding non-essential calculations, resulted in an efficient and accurate IM model implementation, that preserves the combined strengths of the DQ and PD formulations.